

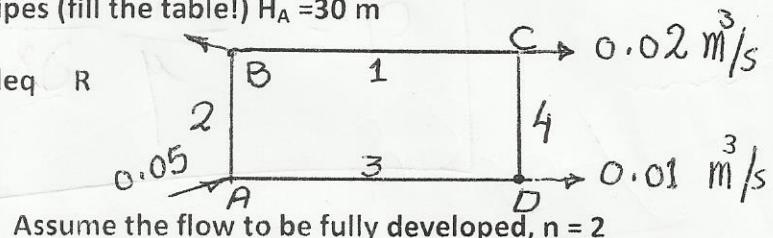
1) Choose the most appropriate statement for each of the following statement

- a) for fully turbulent pipe flow the friction coefficient f is function of 1) Reynolds number only. 2) both Re and relative roughness ϵ/D . 3) ϵ/D only
- b) Separation may take place if the pressure gradient is 1) zero. 2) positive. 3) negative
- c) The pressure increase due to sudden valve closure equals 1) $\rho V^2/2$ 2) $\rho V C$ 3) $2\rho VL/t_c$

2 - Use Hardy Cross method to find the discharge in each pipe and the head at B and D.

Given below are the characteristics of pipes (fill the table!) $H_A = 30 \text{ m}$

Pipe	ϵ/D	L m	D cm	Σk	I_{eq}	R
1,3	0.001	50	20	2		
2,4	0.001	30	20	4		



3) Use Navier -Stokes equation for 2-dimensional incompressible steady developed flow between two parallel fixed plates separated by a distance b to show that

$$u = \frac{1}{2} \left(\frac{dpb^2}{dx\mu} \right) \left[\left(\frac{y}{b} \right)^2 - \left(\frac{y}{b} \right) \right]$$

Evaluate the discharge in a duct 100 cm wide and 30 cm deep if the pressure drop is 4.27 Pa per 100 m length of duct. Viscosity is $2.4 \times 10^{-5} \text{ Pa.s}$ neglect end effects.

(3-b) Velocity profile in a boundary layer is given by $\frac{u}{U} = a + b \frac{y}{\delta} + c \left(\frac{y}{\delta} \right)^2$ Find a,b, and c to satisfy the boundary conditions.

4-a Explain briefly the followings:

- a) Water hammer phenomena.
- B) Harmful effect of Water hammer.

4-b Water is flowing in a pipe of 150 mm diameter D with velocity of 2.5 m/s, when it is suddenly brought to rest by closing the valve. Find the pressure rise assuming pipe is elastic, $E=206 \text{ GN/m}^2$, Poisson ratio 0.25 and K for water = 2.06 GN/m^2 . Pipe wall thickness $t = 5 \text{ mm}$. Expansion joints are used every where

$$C^2 = \frac{K/\rho}{1 + (K/E)(D/t)} \quad \text{Where } C \text{ is the wave speed}$$

Faculty of Engineering at shoubra

Fluid Dynamics 2nd- year power

Model Answer of [Mid-Term exam]

April 2013

1- choose the most appropriate statement For each of the following statement:-

- a- For fully turbulent pipe flow the friction coefficient f is function of $\frac{\epsilon}{D}$ only.
- b- Separation may take place if the pressure gradient is positive.
- c- ~~The~~ the pressure increase due to sudden valve closure equal $\rho V^2 C$

2. Find discharge in each pipe [1, 2, 3, 4]

and H_B, H_D

pipe	$\frac{\epsilon}{D}$	L(m)	D(cm)	ζK	F	L_{eqv}	R
1,3	0.001	50	20	2	0.02	20	361.8
2,4	0.001	30	20	4	0.02	40	361.8

- $h_{major} = h_{minor}$

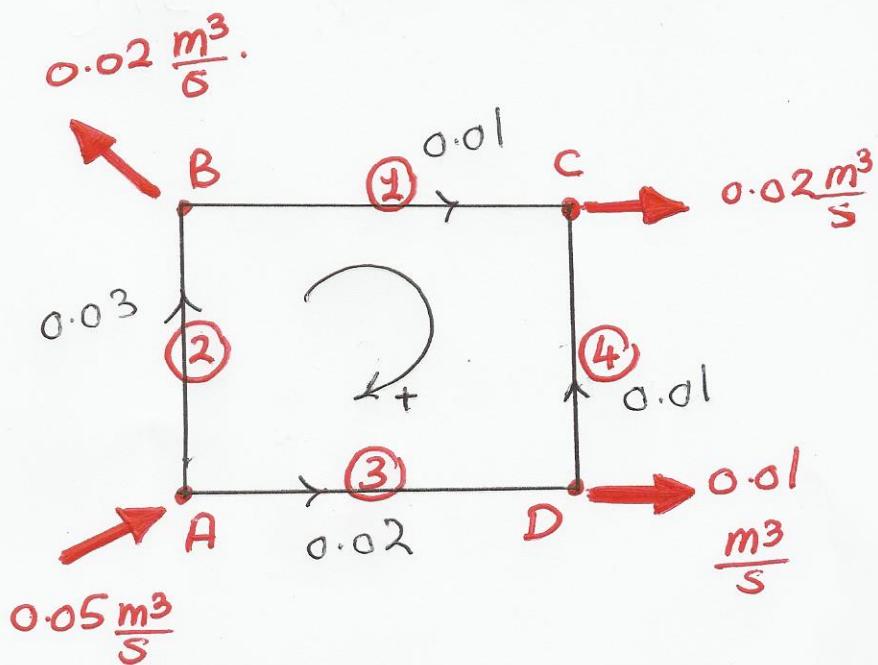
$$\frac{f \cdot L}{D} \frac{V^2}{2g} = \zeta K \frac{V^2}{2g} \rightarrow \therefore L_{eqv} = \frac{\zeta K \cdot D}{F} \rightarrow \boxed{1}$$

$$\rightarrow R = \frac{8F(L + L_{eqv})}{\pi^2 \cdot g \cdot D^5} \rightarrow \boxed{2}$$

From moody chart

by using $\frac{\epsilon}{D} = 0.001$

$$\therefore f = 0.02$$



pipe	Q	R	RQ^2	$2RQ$
1	0.01	361.8	0.03618	7.236
2	0.03	361.8	0.32562	21.708
3	-0.02	361.8	0.14472	14.472
4	-0.01	361.8	-0.03618	7.236

$$\downarrow \sum RQ^2 = \quad \downarrow \sum 2RQ =$$

$$\therefore \Delta Q = -\frac{\sum RQ^2}{\sum 2RQ}$$

$$= -\frac{0.1809}{50.652} = -0.0035$$

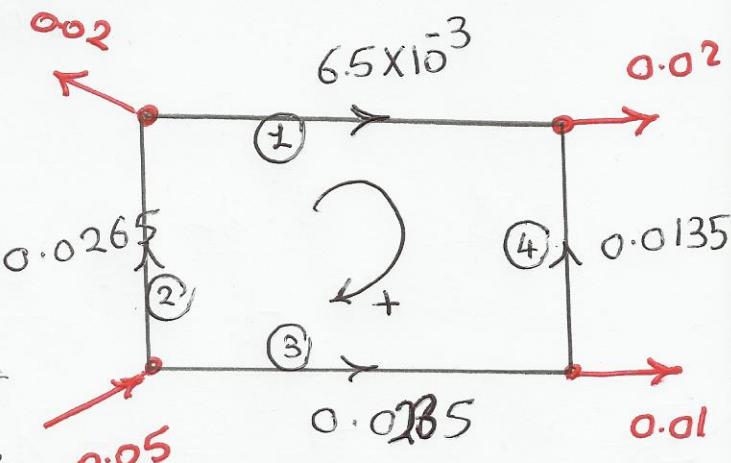
pipe	Q	R	RQ^2	$2RQ$
1	+0.0065	361.8	+0.0152	4.9034
2	+0.0265	361.8	+0.254	19.1754
3	-0.0235	361.8	-0.1998	17.0046
4	-0.0135	361.8	-0.0659	9.7686

$$\downarrow \sum 2RQ = 50.652$$

$$\sum RQ^2 = 3.5 \times 10^{-3}$$

$$\therefore \Delta Q = -\frac{\sum RQ^2}{\sum 2RQ}$$

$$= -\frac{3.5 \times 10^{-3}}{50.625} = -6.9 \times 10^{-5}$$

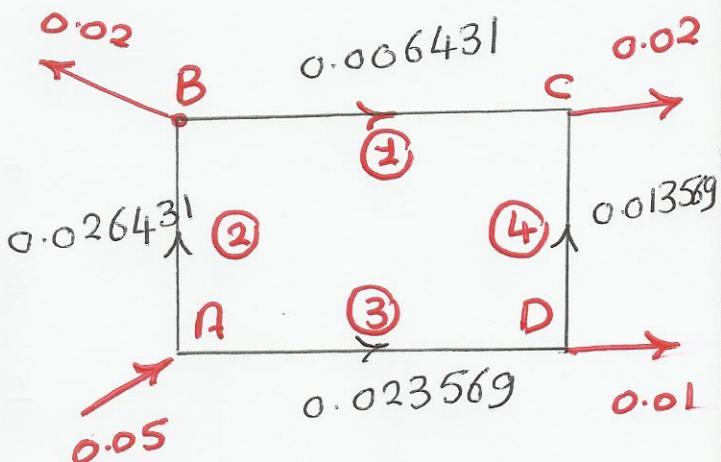


$$\therefore Q_1 = 0.006431 \frac{m^3}{s}$$

$$Q_2 = 0.026431 \frac{m^3}{s}$$

$$Q_3 = 0.023569 \frac{m^3}{s}$$

$$Q_4 = 0.013569 \frac{m^3}{s}$$



For pipe no. 2

$$H_A - H_B = R \frac{Q^2}{2} \Rightarrow H_B = H_A - R Q^2 \\ = 30 - 361.8 (0.026431)^2 \\ = 29.74 \text{ m}$$

For pipe no. 3

$$H_D = H_A - R \frac{Q^2}{3} = 30 - (361.8)(0.023569)^2 \\ = 29.79 \text{ m.}$$

3. Solution :-

using navier-stokes equation

$$\cancel{\rho} \left[\cancel{\frac{\partial u}{\partial t}} + u \cancel{\frac{\partial u}{\partial x}} + v \cancel{\frac{\partial u}{\partial y}} + w \cancel{\frac{\partial u}{\partial z}} \right] = - \frac{\partial P}{\partial x} + \gamma \left[\cancel{\frac{\partial^2 u}{\partial x^2}} + \cancel{\frac{\partial^2 u}{\partial y^2}} + \cancel{\frac{\partial^2 u}{\partial z^2}} \right].$$

$$\therefore \frac{1}{\gamma} \frac{\partial P}{\partial x} = \frac{\partial^2 u}{\partial y^2} \Rightarrow \therefore \frac{\partial u}{\partial y} = \frac{1}{\gamma} \frac{\partial P}{\partial x} y + C_1$$

$$\Rightarrow \therefore u(y) = \frac{1}{\gamma} \frac{\partial P}{\partial x} \frac{y^2}{2} + C_1 y + C_2$$

To get the B.C's

$$\text{at } y=0 \rightarrow u=0 \Rightarrow C_2 = 0$$

$$\text{at } y=b \rightarrow u=0$$

$$\therefore 0 = \frac{1}{\gamma} \frac{\partial P}{\partial x} \frac{b^2}{2} + C_1 \cancel{y}$$

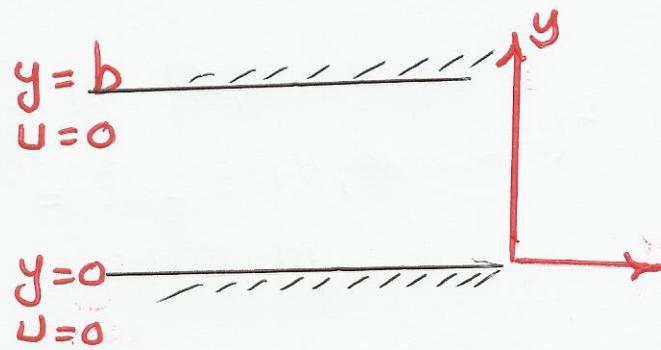
$$\therefore C_1 = - \frac{1}{2\gamma} \frac{\partial P}{\partial x} b$$

$$\therefore u(y) = \frac{1}{2\gamma} \frac{\partial P}{\partial x} y^2 - \frac{1}{2\gamma} \frac{\partial P}{\partial x} b \cdot y$$

$$\therefore u(y) = \frac{1}{2} \left(\frac{\partial P}{\partial x} \cdot \frac{b^2}{\gamma} \right) \left[\frac{y^2}{b^2} - \frac{y}{b} \right] \cancel{b}$$

$$\begin{aligned} \text{• Discharge (Q)} &= \int u(y) \cdot dy = \frac{\partial P}{\partial x} \frac{b^2}{2\gamma} \left[\frac{y^3}{3b^2} - \frac{y^2}{2b} \right]_0^b \\ &= \frac{b^2}{2\gamma} \frac{\partial P}{\partial x} \left[\frac{b}{3} - \frac{b}{2} \right] = - \frac{1}{12} \frac{b^3}{\gamma} \frac{\partial P}{\partial x} \end{aligned}$$

$$\therefore Q = - \frac{1}{12} \frac{(30 \times 10^{-2})^3}{2.4 \times 10^{-5}} \cdot \left(\frac{-4.27}{100} \right) = 4.003 \frac{m^3}{s}.$$



$$\underline{3-b} \quad \frac{v}{U} = a + b\left(\frac{y}{\delta}\right) + c\left(\frac{y}{\delta}\right)^2 \quad \text{Find } a, b, c$$

• at $y=0 \rightarrow v=0 \Rightarrow a=0 \quad \#$

• at $y=\delta \rightarrow v=U \Rightarrow 1 = \cancel{a} + b + c$

$$\therefore 1 = b + c \rightarrow ①$$

• at $y=\delta \rightarrow \frac{\partial v}{\partial y} = 0$

$$\frac{\partial \left(\frac{v}{U}\right)}{\partial \left(\frac{y}{\delta}\right)} = 0 \quad \therefore 0 = b + 2c$$

$$\therefore b = -2c$$

$$\therefore 1 = -2c + c$$

$$\therefore c = -1 \quad \#$$

$$\therefore b = 2 \quad \#$$

4.g Explain briefly the following

a- water hammer phenomena

is a pressure surge or wave caused when fluid in motion is forced to stop or change direction suddenly

B- Harmful effect of water hammer.

- Damage in Equipments.
- pipe broken
- Reverse pressure.

4.b

$D = 150 \text{ mm}$. Find ΔP

$$v = 2.5 \frac{\text{m}}{\text{s}}$$

$$E = 206 \text{ GN/m}^2$$

$$\gamma = 0.25$$

$$k = 2.06 \frac{\text{GN}}{\text{m}^2}$$

$$t = 5 \text{ mm}$$

$$C^2 = \frac{K/\beta}{1 + \left(\frac{K}{E}\right)\left(\frac{D}{t}\right)} = \frac{(2.06 \times 10^9)/1000}{1 + \left(\frac{2.06}{206}\right)\left(\frac{150}{5}\right)}$$

$$= 1584615.385$$

$$\therefore C = 1258.81 \frac{\text{m}}{\text{s}}$$

$$\therefore \Delta P = \rho v C$$

$$= 1000 \times 2.5 \times 1258.81 = 3147037.679 \frac{\text{Pa}}{\text{Pa}}$$

$$= 3147.03 \text{ kPa}$$